

Эксклюзивное рождение π^+ в эксперименте на установке ГЕРМЕС

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Сессия-конференция секции ядерной физики ОФН РАН
Протвино, 22-25 декабря, 2008

- ▶ Generalised Parton Distributions
- ▶ Exclusive π^+ production at HERMES
 - ▶ Cross section measurements and results
 - ▶ Preliminary study of transverse spin asymmetry

Generalised Parton Distributions

- in the limit of $Q^2 \gg$ at x_B , t fixed, $\gamma^* p$ amplitude factorises

- contributions to the cross section

γ_L^* leading-twist, QCD factorisation theorem

$\gamma_L^* - \gamma_T^*$ $\frac{1}{Q}$ suppressed

γ_T^* $\frac{1}{Q^2}$ suppressed

- for exclusive π^+ production $\gamma^* p \rightarrow \pi^+ n$

$$\sigma_L \propto (1 - \xi^2) |\tilde{H}|^2 - \xi^2 t |\tilde{E}|^2 - \xi^2 \text{Re}(\tilde{E}^* \tilde{H})$$

ξ : skewness

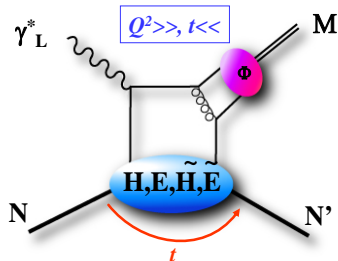
- relation to PDFs and FFs

$$\tilde{H}(x, 0, 0) = \Delta q(x) \text{ for } t \rightarrow 0$$

$$\int_{-1}^1 dx \tilde{H}(x, \xi, t) = g_A(t)$$

$$\int_{-1}^1 dx \tilde{E}(x, \xi, t) = g_P(t)$$

- how to access GPDs?



- exclusive production of

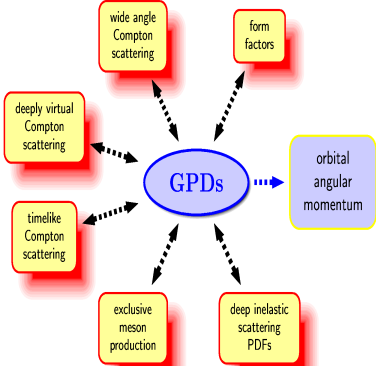
$$\gamma \rightarrow H, E, \tilde{H}, \tilde{E}$$

$$\rho, \omega, \phi \rightarrow H, E$$

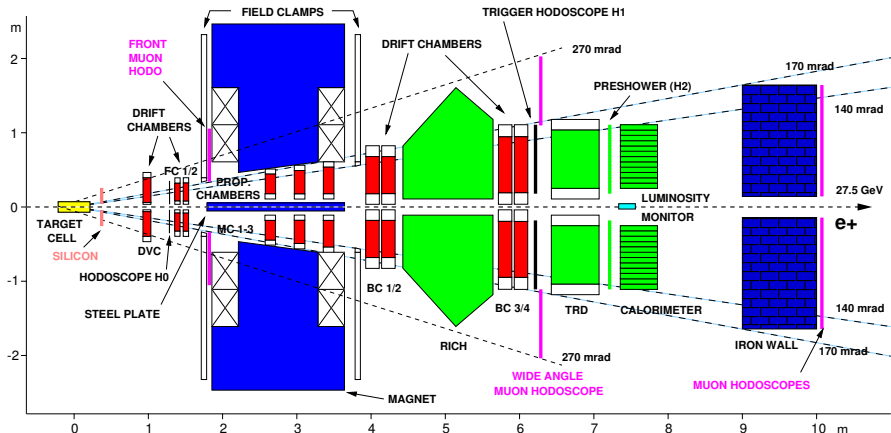
$$\pi, \eta \rightarrow \tilde{H}, \tilde{E}$$

- ! no precocious scaling at $Q^2 \geq 1 \text{ GeV}^2$ for hard exclusive meson production

GPD



The HERMES experiment at DESY



- internal (polarised) hydrogen fixed target, 27.6 GeV (polarised) e^\pm beam
1.5 T m,
- tracking system: drift chambers $\Delta\theta = 0.6$ mrad, vertical dipole magnet $\frac{\Delta p}{p} = 0.5\%$
- lepton-hadron separation: > 99% efficiency; particle identification: π , $p_\pi = 1-15$ GeV

Exclusivity for $ep \rightarrow e'\pi^+n$ at HERMES

- no recoil detection

⇒ missing mass technique:

$$M_X^2 = (q_e + q_p - q_{e'} - q_{\pi^+})^2$$

for $(N_{\pi^+} - N_{\pi^-})^{\text{data}}$

for $(N_{\pi^+} - N_{\pi^-})^{\text{PYTHIA}}$

⇒ $N_{\pi^+}^{\text{excl}}$ obtained as a
double difference

PYTHIA Monte Carlo generator:

-no nucl.res. and excl. π^+ processes
-tuned to HERMES SIDIS and VM
prod.

- kinematic requirements

$$Q^2 > 1 \text{ GeV}^2$$

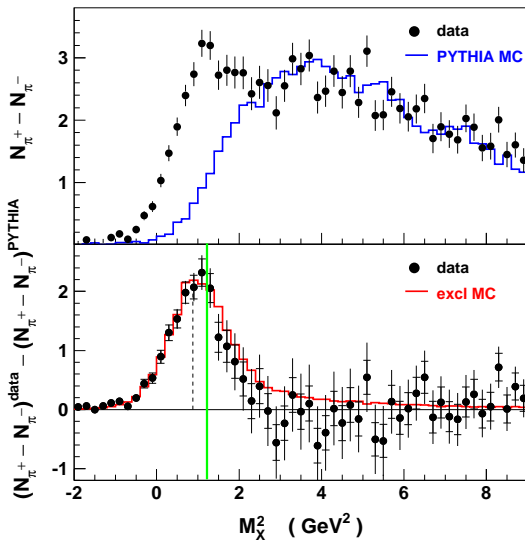
$$W^2 > 10 \text{ GeV}^2$$

$$y < 0.85$$

$$p_{\pi} > 7 \text{ GeV}$$

- $M_X^2 < 1.2 \text{ GeV}^2$

$$t' = t - t_0$$



Exclusive peak clearly centred at the neutron mass
Mean and width in agreement with exclusive MC

Cross section determination

- $ep \leftrightarrow \gamma^* p$: $\frac{d\sigma^{\gamma^* p \rightarrow \pi^+ n}(x_B, Q^2, t', \phi)}{dt' d\phi} = \frac{1}{\Gamma_V(x_B, Q^2)} \frac{d\sigma^{ep \rightarrow e' \pi^+ n}(x_B, Q^2, t', \phi)}{dx_B dQ^2 dt' d\phi}$
- Hand convention: $\Gamma_V(x_B, Q^2) = \frac{\alpha}{8\pi} \frac{1}{M_p^2 E^2} \frac{Q^2}{x_B^3} \frac{1-x_B}{1-\epsilon}$, ϵ : γ^* polarisation parameter

$N_{\pi^+}^{excl}$ π^+ events after background subtr.

Γ_V virtual-photon flux factor

\mathcal{L} integrated luminosity

κ detection probability

η radiative correction factor

Δ bin size

For the data sample 1996-2005:

- $N_{\pi^+}^{excl} = 4510$ events, $[2 - 20\%]_{\text{sys}}$ $\mathcal{L} = 0.4 \text{ fb}^{-1}$ $[5\%]_{\text{sys}}$

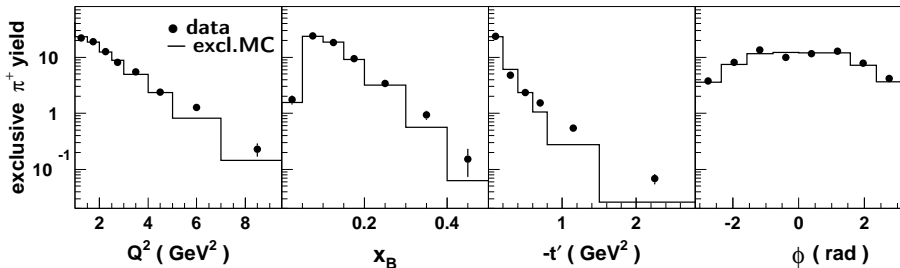
- kinematic range

$$1 < Q^2 < 11 \text{ GeV}^2 \quad \rightarrow \quad \text{four } Q^2 \text{ bins}$$

$$0.02 < x_B < 0.55 \quad \rightarrow \quad \text{three } x_B \text{ bins}$$

$$0 < -t' < 3 \text{ GeV}^2 \quad \rightarrow \quad \text{six } -t' \text{ bins}$$

Exclusive distributions: Monte Carlo comparison



exclusive MC (GPD models):

• Vanderhaeghen, Guichon, Guidal [PRD60\(1999\)094](#)

or

○ Mankiewicz, Piller, Radyushkin

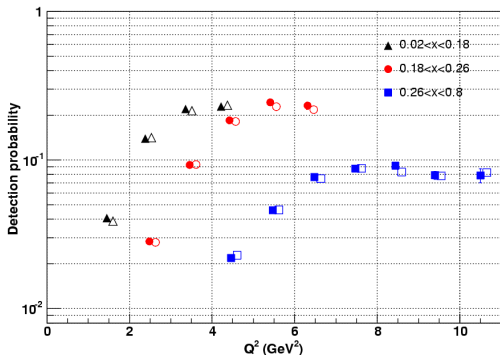
[EPJC10\(1999\)307](#)

$$\kappa = \frac{N_{\pi^+}^{rec}}{N_{\pi^+}^{gen}} = [0.04 - 0.28] \quad \begin{array}{l} \text{acc. [0.1-0.7]} \\ \text{cuts [0.4-0.5]} \end{array}$$

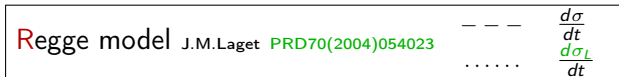
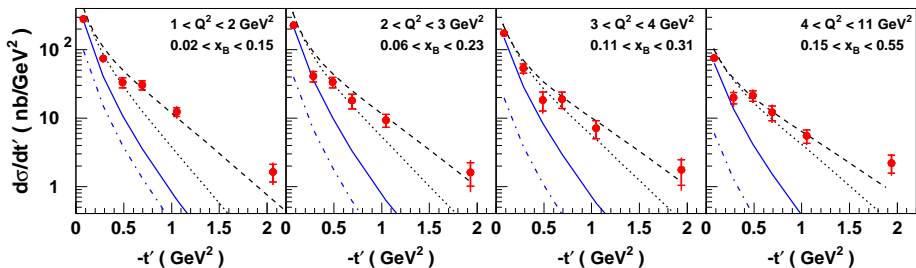
κ : probability to detect e' and π^+ (generated in 4π) in the HERMES spectrometer; [$\sim 15\%$]_{sys}

$$\eta = \frac{\sigma^{obs}}{\sigma^{Born}} = 0.77, \text{ at } M_X^2 < 1.2 \text{ GeV}^2$$

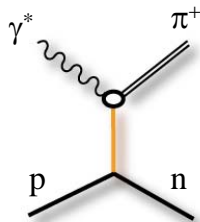
-dominated by vertex&loop corrections
-independent of kinematics



Results: the differential cross sections PLB659(2008)486

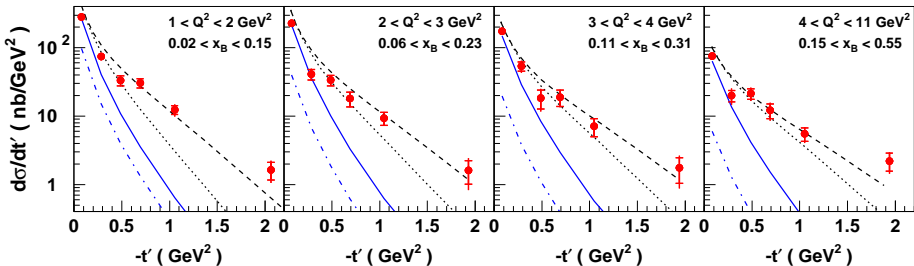


- ▶ π^+ production described by exchange of π and ρ Regge trajectories
- ▶ Q^2 - and $-t'$ -dependent FFs for $\pi\pi\gamma$ and $\pi\rho\gamma$
- ▶ σ_T predicted to be 15-25% of σ (about 6% at low $-t'$)



good description of the magnitude, and $-t'$, Q^2 dependences of the data

Comparison with theory PLB659(2008)486

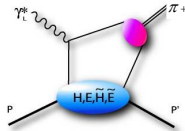
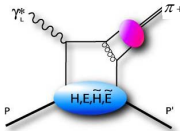


GPD model for $\frac{d\sigma_L}{dt'}$

- · - leading-order calculations
- with power corrections

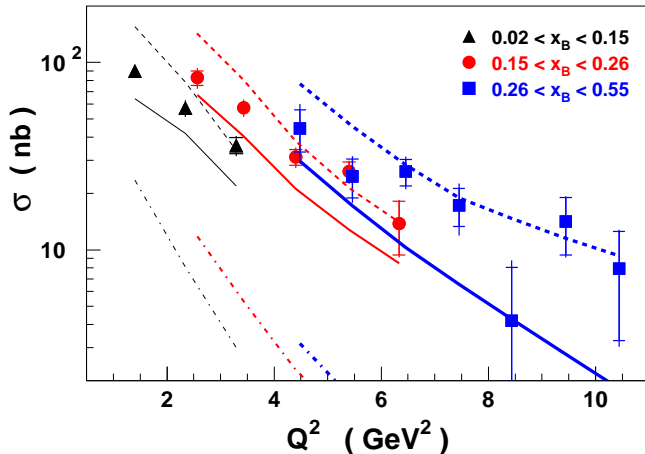
Vanderhaeghen, Guichon, Guidal PRD60(1999)094017

- ▶ \tilde{E} dominated by pion-pole, F_π
- ▶ \tilde{H} neglected
- ▶ Regge-inspired t dependence for \tilde{E}
- ▶ power corrections due to intrinsic k_T and **soft-overlap** contribution



fair agreement with data at lower $-t'$ if power corrections are included

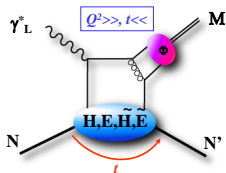
Results: the total cross section PLB659(2008)486



| | | |
|-------------|-----|----------------------------|
| GPD model | --- | leading-order calculations |
| | — | with power corrections |
| Regge model | --- | Regge model for σ |

GPD model: fair agreement, Regge model: good description of data

Transverse spin asymmetry

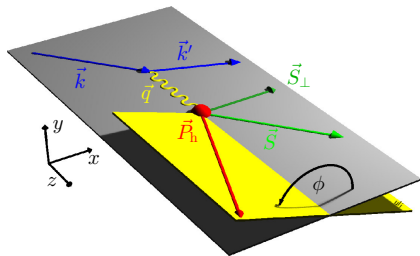


unp. cross section
spin asymmetry

$$\sigma_{UU} \propto |\tilde{H}|^2 - t|\tilde{E}|^2 - \text{Re}(\tilde{E}^*\tilde{H})$$

$$\propto \text{Im}(\tilde{E}^*\tilde{H})/\sigma_{UU}$$

higher order corrections cancel
scaling reached at lower Q^2



For transversely polarised target:

$$\sigma_{UT} \propto |\vec{S}_T| \sin(\phi - \phi_S) \text{Im}(\tilde{E}^*\tilde{H}) + \dots$$

\Rightarrow extract $A_{UT}^{\sin(\phi - \phi_S)}$ plus additional
five sine amplitudes

M. Diehl, S. Sapeta EPJC41(2005)515

Transverse spin asymmetry

$$\mathcal{A}_{UT} = \frac{1}{|\mathbf{P}_T|} \frac{d\sigma(\phi, \phi_S) - d\sigma(\phi, \phi_S + \pi)}{d\sigma(\phi, \phi_S) + d\sigma(\phi, \phi_S + \pi)}$$

M. Diel and S. Sapeta, Eur. Phys. J. C 41 (2005) 515 :

$$\begin{aligned} & \mathcal{A}_{UT}(\phi, \phi_S; \eta_{UT}) \\ &= A_{UT}^{\sin(\phi - \phi_S)} \sin(\phi - \phi_S) + A_{UT}^{\sin(\phi + \phi_S)} \sin(\phi + \phi_S) \\ &+ A_{UT}^{\sin\phi_S} \sin\phi_S + A_{UT}^{\sin(2\phi - \phi_S)} \sin(2\phi - \phi_S) \\ &+ A_{UT}^{\sin(3\phi - \phi_S)} \sin(3\phi - \phi_S) + A_{UT}^{\sin(2\phi + \phi_S)} \sin(2\phi + \phi_S) \end{aligned}$$

Measured asymmetry A_{UT} vs. squared missing mass

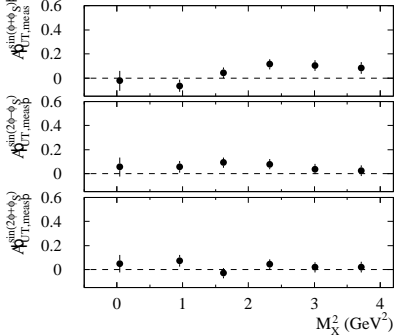
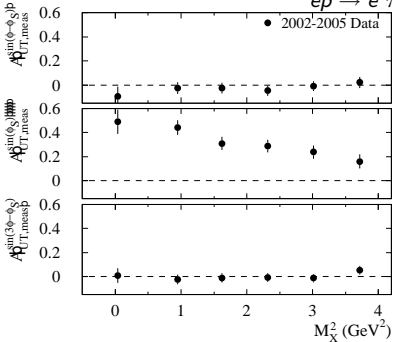
measured = exclusive signal plus background

$f_{\pi^+}^{excl} = \frac{N_{\pi^+}^{excl}}{N_{\pi^+}^{data}} \approx \frac{1}{2}$

A_{UT} in $M_X^2 = [0.5 - 1.2] \text{ GeV}^2$

$A_{UT,bg}$ in $M_X^2 = [1.9 - 3.3] \text{ GeV}^2$

$ep \rightarrow e' \pi^+ X$



► background correction → extract exclusive asymmetry

$$A_{UT,\pi^+}^{excl} \equiv A_{UT,bg.corr} = \frac{1}{f_{\pi^+}^{excl}} A_{UT} - \frac{1 - f_{\pi^+}^{excl}}{f_{\pi^+}^{excl}} A_{UT,bg}$$

Kinematic dependences of A_{UT,π^+}^{excl}

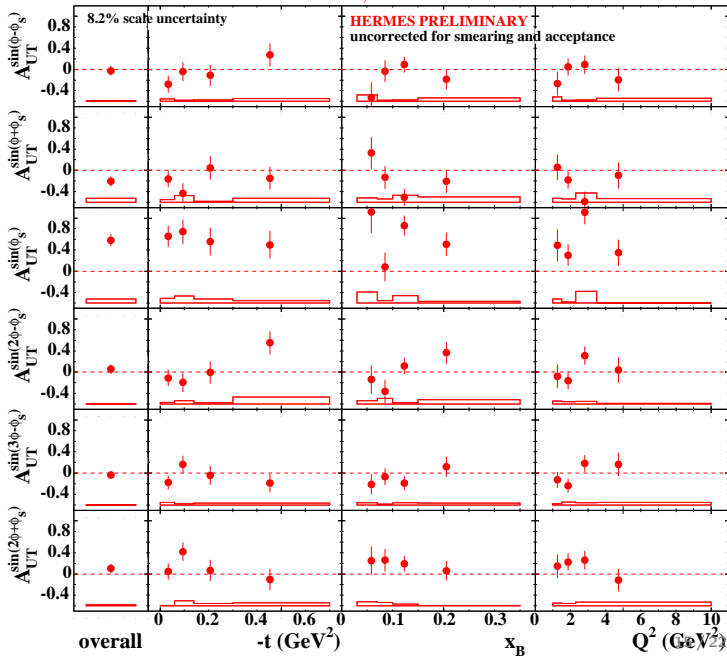
$$ep \rightarrow e'\pi^+n$$

$$-t \equiv -t'$$

$$\langle -t \rangle = 0.182 \text{ GeV}^2$$

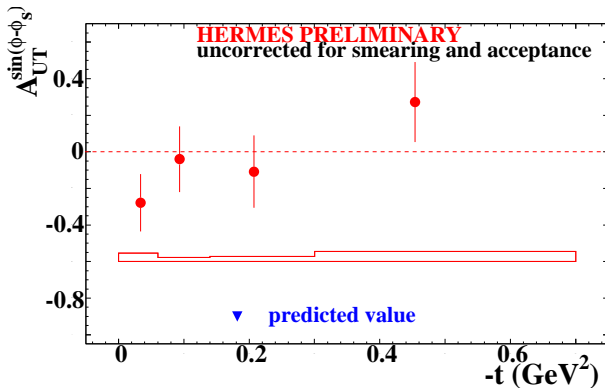
$$\langle x \rangle = 0.126$$

$$\langle Q^2 \rangle = 2.38 \text{ GeV}^2$$



Leading asymmetry amplitude $A_{UT}^{\sin(\phi-\phi_S)}$ vs. $-t$

- ▶ measurement indicates a sign change over $-t$ or consistency with zero
- ▶ cross section results indicate power corrections to \tilde{E} are important
 - ▶ therefore \tilde{E} increases substantially
 - ▶ but \tilde{H} remains small



$\Rightarrow A_{UT}^{\sin(\phi-\phi_S)}$ measurement consistent with cross section result

Summary and conclusions

Exclusive π^+ cross section

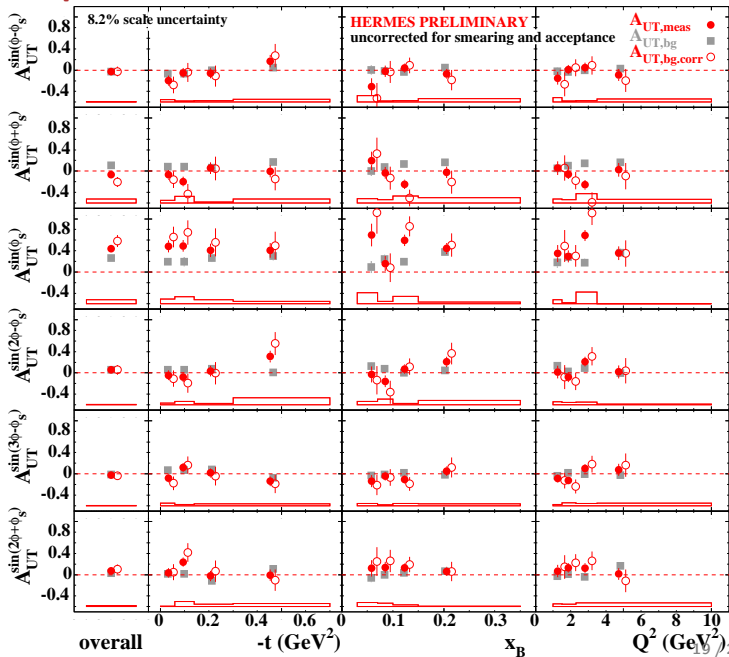
- ▶ results from recent paper [PLB 659 \(2008\) 486](#)
- ▶ cross section result indicates small σ_T contribution
- ▶ GPD model in fair agreement with data at low values of $-t$; data support the order of magnitude of power corrections
- ▶ Regge model provides good description of the kinematic dependences

Transverse spin asymmetry

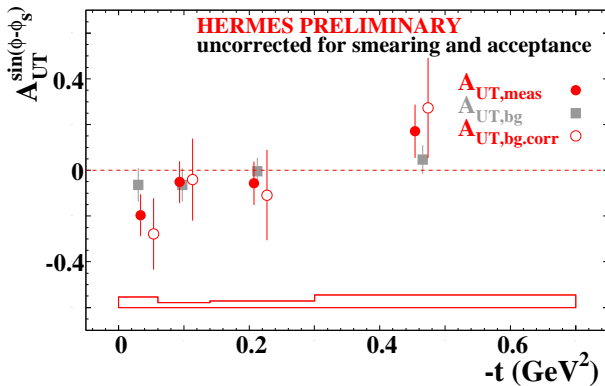
- ▶ preliminary results
- ▶ first experimental attempt to study this observable
- ▶ the leading asymmetry amplitude is compared to theoretical calculations: smaller asymmetry than predicted by theory
- ▶ supposedly $\tilde{E} \gg \tilde{H}$
- ▶ larger statistics required for more detailed studies of the kinematic dependences, for example @ JLab

Backup slides

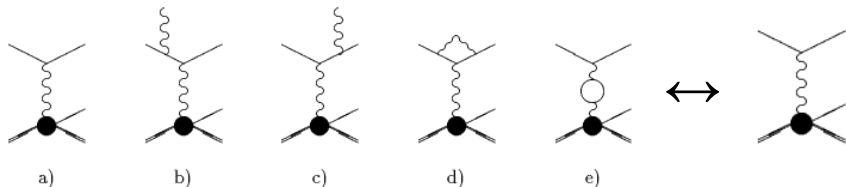
Kinematic dependences of A_{UT}



$A_{UT}^{\sin(\phi-\phi_s)}$ vs. $-t$

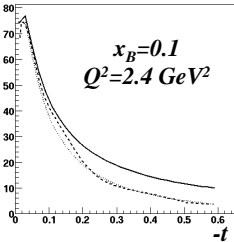
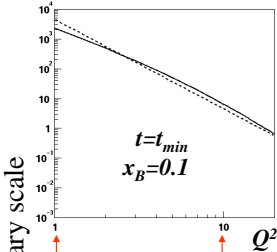


Radiative effects for exclusive π^+ production



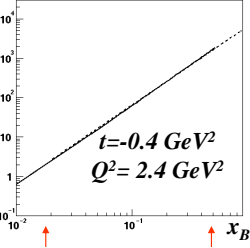
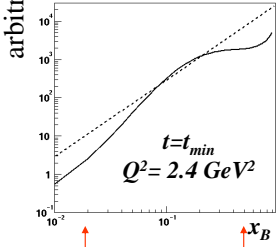
- correct the measured cross section by $\eta = \frac{\sigma^{obs}}{\sigma^{Born}} = 0.77$
- RADGEN adapted to exclusive processes with VGG GPD model as input
Akushevich, Böttcher, Ryckbosch [hep-ph/9906408](https://arxiv.org/abs/hep-ph/9906408), A. Ilyichev
- little variation of η ($< 3\%$) as a function of x_B , Q^2 , or t' for $M_x^2 < 1.2 \text{ GeV}^2$
- compute at Born level $\langle x_B \rangle$, $\langle Q^2 \rangle$, $\langle t' \rangle$, $\Gamma_V(\langle x_B \rangle, \langle Q^2 \rangle)$
- corrections applied for smearing $12/15\%$ ($< 25/35\%$), bin size $\delta = 1.08$ (< 1.2)

GPD models



— VGG model
 Tuned VGG ($\tilde{E}^* e^t$)
 - - Piller model

↑ ↑ Hermes kinematics



→ different dependence for VGG and Piller

- ▶ VGG model: Vanderhaeghen, Guichon, Guidal [PRD 60 \(1999\) 094017](#)
- ▶ Piller model: Mankiewicz, Piller, Radyushkin [EPJC 10 \(1999\) 307](#)